

# **Programming Abstractions**

**Week 13-1: Streams**

**Stephen Checkoway**

What is printed by this code?

```
(let* ([x 10]  
      [y x])  
  (set! x 20)  
  (displayln y))
```

A. 10

B. 20

C. It's an error

What is printed by this code?

```
(let* ([x 10]
       [y (delay x)])
  (set! x 20)
  (displayln (force y)))
```

A. 10

B. 20

C. It's an error

What is printed by this code?

```
(let* ([x 10]
       [y (delay x)])
  (set! x 20)
  (displayln (force y))
  (set! x 30)
  (displayln (force y)))
```

A. 20  
20

B. 20  
30

C. 30  
30

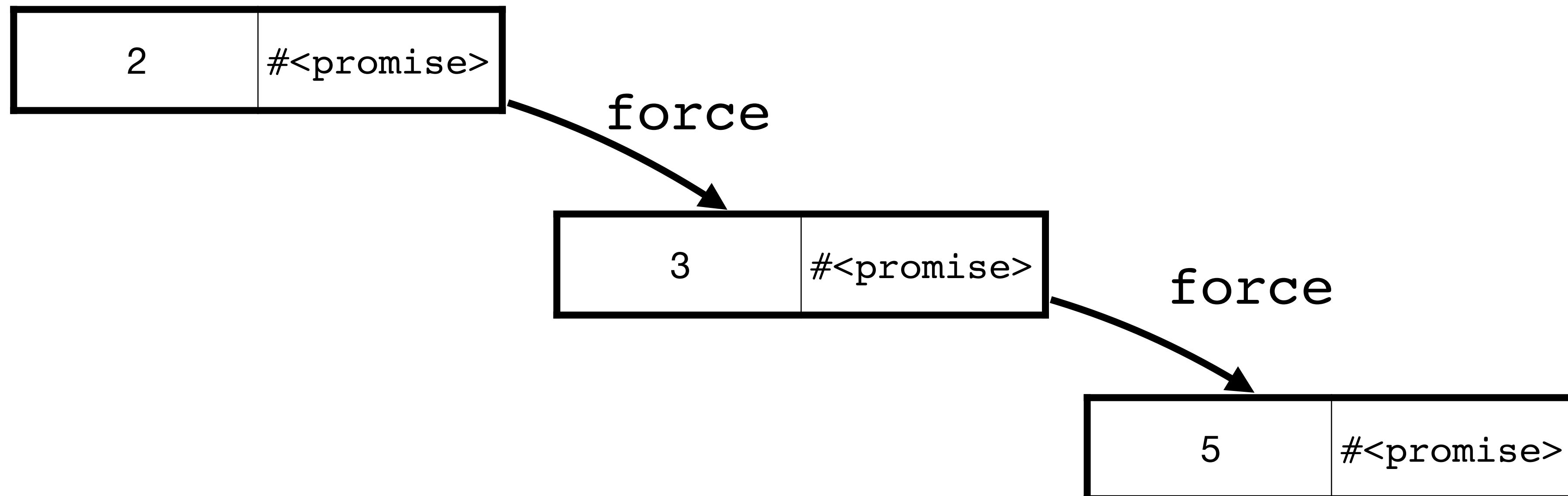
D. It's an error

# Last time: infinite list of primes

First, we need to think about how we want to represent this

Let's use a cons cell where

- ▶ the `car` is a prime; and
- ▶ the `cdr` is a promise which will return the next cons cell



# An infinite list is an instance of a stream

A stream is a (possibly infinite) sequence of elements

A list is a valid, finite stream

▸ `(stream? '(1 2 3)) => #t`

Infinite streams must be built lazily out of promises (using `delay` internally)

Accessing elements of a stream forces their evaluation

# Let's build a stream

As with our infinite list of primes we'll use a cons-cell holding a value and a promise

## API

- ▶ `(stream-cons head tail)`
- ▶ `(stream-first s)`
- ▶ `(stream-rest s)`
- ▶ `(stream-empty? s)`
- ▶ `empty-stream`

# Constructing a lazy stream

```
(stream-cons head tail)
```

We can't use a procedure because it'll evaluate `head` and `tail`

```
(define-syntax stream-cons
  (syntax-rules ()
    [(_ head tail) (delay (cons head (delay tail)))]))
```

`stream-cons` returns a `promise` which when forced gives a `cons` cell where the second element is a `promise`



# Accessing the stream

```
(stream-first s) (stream-rest s)
```

`s` is either a promise or a cons cell so we need to check which

```
(define (stream-first s)
  (if (promise? s)
      (stream-first (force s))
      (car s)))
```

```
(define (stream-rest s)
  (if (promise? s)
      (stream-rest (force s))
      (cdr s)))
```

We can't use `first` and `rest` because those check if their arguments are lists

# Checking if a stream is empty

```
(define empty-stream null)
(define (stream-empty? s)
  (if (promise? s)
      (stream-empty? (force s))
      (null? s)))
```

# Constructing an infinite stream

Write a procedure which

- returns a stream constructed via `stream-cons`
- where the tail of the stream is a `recursive call` to the procedure

Call the procedure with the initial argument

```
(define (integers-from n)
  (stream-cons n (integers-from (add1 n))))
```

```
(define positive-integers (integers-from 0))
```

# Accessing the elements

We can use `stream-first` and `stream-rest` to iterate through the elements

```
(define (stream-ref s idx)
  (cond [(zero? idx) (stream-first s)]
        [else (stream-ref (stream-rest s) (sub1 idx))]))
```

# Primes as a stream

```
(define (prime? n) ...) ; Same as last time
```

```
(define (next-prime n)
  (cond [(prime? n) (stream-cons n (next-prime (+ n 2)))]
        [else (next-prime (+ n 2))]))
```

```
(define (primes)
  (stream-cons 2 (next-prime 3)))
```

# Fibonacci numbers as a stream

Recall the Fibonacci numbers are defined by  $f_0 = 0$ ,  $f_1 = 1$  and  $f_n = f_{n-1} + f_{n-2}$

```
(define (next-fib m n)
  (stream-cons m (next-fib n (+ m n))))
```

```
(define fibs (next-fib 0 1))
```



# Fibonacci numbers as a stream: take 2

$$f_0 = 0, f_1 = 1 \text{ and } f_n = f_{n-1} + f_{n-2}$$

We can build our Fibonacci sequence directly from that definition (this is silly)

```
(define fibs
  (stream-cons
    0
    (stream-cons
      1
      (stream-add fibs (stream-rest fibs)))))
```



# Streams in Racket

These are already built-in so we don't need to write them

- `(require racket/stream)`
- `(stream exp ...)` ; Works like `(list exp ...)`
- `(stream? v)`
- `(stream-cons head tail)`
- `(stream-first s)`
- `(stream-rest s)`
- `(stream-empty? s)`
- `empty-stream`
- `(stream-ref s idx)`

And several others

# Let's write some Racket!

Open up a new file in DrRacket

Make sure the top of the file contains

```
#lang racket  
(require racket/stream)
```

Write the procedure `(stream-length s)` which returns the length of a finite stream

i.e., `(stream-length (stream 1 2 3 4 5))` returns 5

Use `stream-empty?` and `stream-rest`

# Write more stream procedures

Write the procedure `(stream->list s)` that takes a finite-length stream and returns the elements as a list

Write the following procedures that act like their list counterparts, but operate lazily on streams; in particular, do not cover them to lists!

- ▶ `(stream-take s num)`  
Returns a stream containing the first `num` elements of `s`, make sure this is lazy
- ▶ `(stream-drop s num)`  
Returns a stream containing all of the elements of `s` in order *except* for the first `num`
- ▶ `(stream-filter f s)`  
Returns a stream containing the elements `x` of `s` for which `(f x)` returns true
- ▶ `(stream-map f s)`  
Returns a stream by mapping `f` over each element of `s`

# Multi-argument stream-map

```
(stream-map f s ...)
```

Racket has `stream-map` built-in but unlike its list counterparts, it only takes a single stream

Generalize it to take any number of streams where the length of the returned string is the minimum length of any of the stream arguments (i.e., return `empty-stream` if any of the streams becomes empty); you'll want to use `ormap`, `map` and `apply`

```
▸ (define (stream-map f . ss) ...)
```